|  |  |  |  |
| --- | --- | --- | --- |
| **I Always Feel Like Somebody’s Watching Me**   |  |  | | --- | --- | | Mary Richardson  Grand Valley State University  [richamar@gvsu.edu](mailto:richamar@gvsu.edu) | Paul Stephenson  Grand Valley State University  [stephenp@gvsu.edu](mailto:stephenp@gvsu.edu) |   **Published: September 2014** | **C:\Users\hstohl\Desktop\JournalEditorialWork\STEW\Website\STEW_logo.gif** |

**Overview of Lesson**

In this activity students will have the opportunity to collect and explore data. Students will perform an experiment in order to test The Psychic Staring Effect. The Psychic Staring Effect is the idea that people can sense that they are being stared at. The activity can be used to illustrate large-sample confidence intervals and hypothesis tests on proportions; two-way table analysis and the chi-square test; the binomial distribution and the binomial test. We have written the activity in three independent parts so that the instructor can choose to complete all three parts of the activity or only one or more of the three parts.

**GAISE Components**

This activity follows all four components of statistical problem solving put forth in the *Guidelines for Assessment and Instruction in Statistics Education (GAISE) Report.* The four components are: formulate a question, design and implement a plan to collect data, analyze the data by measures and graphs, and interpret the results in the context of the original question. All three parts of this activity are at the GAISE Level C.

**Common Core State Standards for Mathematical Practice**

1. Make sense of problems and persevere in solving them.

2. Reason abstractly and quantitatively.

4. Model with mathematics.

5. Use appropriate tools strategically.

6. Attend to precision.

**Common Core State Standard Grade Level Content (High School)**

S-ID. 5. Summarize categorical data for two categories in two-way frequency tables. Interpret relative frequencies in the context of the data (including joint, marginal, and conditional relative frequencies). Recognize possible associations and trends in the data.

S-IC. 1. Understand statistics as a process for making inferences about population parameters based on a random sample from that population.

**NCTM Principles and Standards for School Mathematics**

**Data Analysis and Probability Standards for Grades 9-12**

**Formulate questions that can be addressed with data and collect, organize, and display relevant data to answer them:**

* understand the meaning of measurement data and categorical data, of univariate and bivariate data, and of the term variable;
* compute basic statistics and understand the distinction between a statistic and a parameter.

**Select and use appropriate statistical methods to analyze data:**

* display and discuss bivariate data where at least one variable is categorical.

**Develop and evaluate inferences and predictions that are based on data**:

* understand how sample statistics reflect the values of population parameters and use sampling distributions as the basis for informal inference.

**Understand and apply basic concepts of probability:**

* understand the concepts of sample space and probability distribution and construct sample spaces and distributions in simple cases;
* compute and interpret the expected value of random variables in simple cases.

**Prerequisites**

Before beginning parts A. and B. of this activity, students should have been introduced to general confidence interval and hypothesis testing concepts (i.e. confidence level, interpretation of a confidence interval, null and alternative hypotheses, p-value, and how to make a statistical conclusion). The activities can be used to reinforce specific formulas that have previously been discussed, or to introduce and apply new formulas.

Before beginning part C. of this activity, students should have some exposure to the binomial distribution and also to the general concepts of hypothesis testing.

**Learning Targets**

After completing part A. of this activity, students will be able to construct and interpret a large-sample confidence interval for a proportion. Students will be able to perform a hypothesis test on a proportion and make a conclusion in a problem’s context.

After completing part B. of this activity, students will be able to tally outcomes for two categorical variables into a two-way contingency table. Students will be able to calculate expected counts for the cells within a contingency table and use the counts to calculate a test statistic for performing a chi-square test. Students will be able to perform the test and to use the results to make a conclusion in a problem’s context.

After completing part C. of this activity, students will be able to identify the characteristics of a Binomial experiment. Students will be able to reason about the expected value of a Binomial random variable. Students will have a better understanding of how to calculate a p-value.

**Time Required**

The time required for each part of the activity is roughly one class period (assuming that the data collection is to be performed along with the completion of the respective activity part). If the data has previously been collected then each part of the activity would take roughly 30 minutes.

**Materials Required**

Students will need a pencil and their graphing calculator. The teacher will provide students with the Activity Worksheet (at the end of this lesson) and some mechanism or instructions for incorporating randomness (the calculator could be used for this task).

**Instructional Lesson Plan**

**The GAISE Statistical Problem-Solving Procedure**

**I. Formulate Question(s)**

**The overall question of interest will be the same for all three activity parts.**

Begin the activity by introducing The Psychic Staring Effect. The Background material provided here and on the Activity Sheet was adapted from: <http://en.wikipedia.org/wiki/Staring>.

The Psychic Staring Effect is the idea that people can sense that they are being stared at and it has been studied heavily, by many different researchers, with different results. In 2003, Rupert Sheldrake wrote the controversial book “The Sense of Being Stared At,” which contained a great deal of anecdotal evidence for the phenomenon: “Many people have had the experience of feeling that they are being looked at, and on turning around find that they really are. Conversely, many people have stared at other people's backs, for example in a lecture theater, and watched them become restless and then turn round.”

After students reported the phenomenon to him in the late 19th century, psychologist Edward B. Titchener suggested that the effect was an illusion, and that when a person turned to check whether they were being watched, the initial movement of their head might attract the focus of somebody behind them who was previously only looking in their general direction. By the time the person had turned their head fully, the second person would be looking directly at them, giving the mistaken impression that they had been staring at them all along.

Discuss some Background information about Rupert Sheldrake. The information provided here and on the Activity Sheet was adapted from: <http://www.sheldrake.org/about-rupert-sheldrake>. Rupert Sheldrake is a biologist and author of more than 80 scientific papers and ten books. He was among the top 100 Global Thought Leaders for 2013, as ranked by the Duttweiler Institute, Zurich, Switzerland’s leading think tank. He studied natural sciences at Cambridge University. He then studied philosophy and history of science at Harvard University, before returning to Cambridge, where he took a Ph.D. in biochemistry (1967).

Dr. Sheldrake has performed research in the area of developmental and cell biology. He has also investigated unexplained aspects of animal behavior, including how pigeons find their way home, the telepathic abilities of dogs, cats and other animals, and the apparent abilities of animals to anticipate earthquakes and tsunamis. He subsequently studied similar phenomena in people, including the sense of being stared at, telepathy between mothers and babies, telepathy in connection with telephone calls, and premonitions. Although some of these areas overlap the field of parapsychology, he approaches them as a biologist, and bases his research on natural history and experiments under natural conditions, as opposed to laboratory studies.

Note: Sheldrake’s web page provides additional background materials and also contains additional information that is not presented here.

After introducing The Psychic Staring Effect and Sheldrake, explain to students that the goal is to perform one of Sheldrake’s experiments to see if a statistical analysis of class data supports Sheldrake’s claims.

**II. Design and Implement a Plan to Collect the Data**

**Once the data has been collected it can be used for all three of the activity parts.**

The teacher should divide students into pairs and explain the data collection procedure. One person will be **the Looker** and the other **the** **Subject**. The Subject should sit with his or her back to the Looker and keep his or her eyes closed. Lookers either ‘look’ or do ‘not look’ at the Subjects in a series of 10 trials according to a random sequence. This random sequence can be generated by a random number generator on a calculator or by tossing a fair coin.

The Looker should stand about 3 feet behind the Subject’s back, and either ‘look’ or ‘not look’ at the Subject in accordance with the random sequence of trials. The teacher might wish to instruct the Lookers to look down at the data collection sheet if they are not looking at the Subject on a particular trial. To signal the beginning of each trial, the teacher should give a signal to the entire class, so that all trials are performed simultaneously. The teacher should say “Trial one: begin.” (Since all Lookers are following different random sequences of instructions, the teacher’s voice will give no relevant clues to the Subjects.) The Subject then says “looking” or “not looking”, and the Looker records the looking status and the Subject’s response on the Data Collection Sheet. The Subject should not spend long thinking, but guess quite quickly, 10 seconds are long enough. The Looker should records the Subject’s guess and then proceed to the next trial. For the next trial the teacher should say, “Trial two: begin.” And so on. The same procedure is repeated for all 10 trials.

After the series of 10 trials has been completed, the Lookers hand in their Data Collection Sheets. The Lookers and Subjects then trade places. Each new Looker starts with a new data sheet.

Assuming a class size of 30 students is split into 15 pairs with each student within a pair playing the role of the Looker, 300 total trials would be produced for the class. After all of the trials have been completed collect the results for the pairs via the Data Collection Sheets and tally the class results on the white board.

Note: 300 total trials will be performed; however, we expect the Looker to be Looking at the Subject in only half of these trials. It is this half that will be used for part of the data analysis that follows.

Table 1 contains example results obtained when this activity was performed with 28 students attending class.

Table 1. Example two-way frequency table for class data.

|  |  |  |  |
| --- | --- | --- | --- |
|  | Answer of Subject | | Row Totals |
| Status of Looker | Looking | Not Looking |
| Looking | 66 | 68 | 134 |
| Not Looking | 76 | 70 | 146 |
| Column Totals | 142 | 138 | 280 |

After the class results are tallied onto the white board, students use the data to answer a series of questions designed to determine if the data support the existence of The Psychic Staring Effect. In the following section, we present three ways to analyze the data.

**III. Analyze the Data**

**The data analysis will differ for the three activity parts. We discuss each part thoroughly in the text that follows.**

**A. Large-Sample Confidence Interval and Hypothesis Test on a Proportion**

Explain to students that we wish to make inferences on the population proportion, *p*. In the context of Sheldrake’s experiment *p* is the proportion of the time that someone who is being Looked at can identify that they are being Looked at.

Discuss the following (large sample) formula that will be used to construct a confidence interval for *p*:  whereis the sample proportion of successes, *n* is the sample size, and

is the multiplier (critical value). The assumptions for using this procedure are: (1) The variable of interest is categorical. (2) The data are obtained using randomization. (3) The sample size is sufficiently large such that the sampling distribution of the sample proportion is approximately normal. Specifically,  and 

Discuss the assumptions with students. Have them identify the variable of interest. On each trial, a success will occur if a Subject correctly identifies being Looked at. Thus, the variable of interest is whether or not a correct response was given by a Subject who is being Looked at. Whether or not the Looker is looking at the Subject on a particular trial will be obtained using randomization. The randomization will either be done by flipping a fair coin or generating a random number in order to determine whether or not the Looker does look at a Subject on an individual trial. For a typical class, the number of trials will approach 150, so it is not likely that the sample size requirement will not be met.

Translate the problem from one concerning the variable of interest to one that involves a population proportion. Ask students to identify what the unknown proportion is in this experiment’s context. In this experiment, the population proportion *p* is the proportion of those being Looked at who correctly identify that they are being Looked at. Have the students calculate the sample proportion for the class results. Informally discuss what the value of the sample proportion indicates about the validity of The Psychic Staring Effect.

Ask students to construct a 95% confidence interval for *p* based upon the class data. Once the interval has been constructed, ask students to interpret the interval and to state whether or not they believe that the class data indicates that there is a Psychic Staring Effect.

For the example class data,  the sample proportion of the time that someone who is being Looked at can identify that they are being Looked at is  or .49. For 95% confidence, the *z* multiplier is 1.96. Thus, inserting the class values into the confidence interval formula gives:  Based upon this confidence interval, we can say, with 95% confidence, that the proportion of the time that someone who is being Looked at can identify that they are being Looked at is between .41 and .57. Notice that this interval includes the value of .50, which does not support the existence of The Psychic Staring Effect.

Next, discuss the procedure for performing a large-sample hypothesis test on the value of a population proportion. If we wish to perform a hypothesis test on a proportion, *p*, the corresponding test statistic formula to test  is  where

is the null hypothesized value, is the sample proportion of successes, and *n* is the sample size. The assumptions are the same as for the large-sample confidence interval for

Have a class discussion about the appropriate value to use for and the appropriate alternative hypothesis to use in order to use the class data to test for the existence of The Psychic Staring Effect. Everyone should agree that the null hypothesis should be and the upper-tailed alternative hypothesis should be 

Once the test statistic value has been calculated, ask students to calculate and interpret the

p-value and to make a conclusion in the context of the problem. That is, do the class data indicate the presence of The Psychic Staring Effect?

For the example class data, the test statistic is:  The teacher may wish to note that this test statistic value is very close to 0. A z test statistic of 0 would be obtained if the sample proportion were exactly equal to .50. Since the alternative hypothesis here is upper tailed, the p-value is equal to the area to the right of  under the standard normal distribution curve. This area is approximately equal to .59. Based upon this p-value, the null hypothesis cannot be rejected. Therefore, the data do not provide significant evidence to indicate that the proportion of the time that someone who is being Looked at can identify that they are being Looked at exceeds .50. Or, in other words, the data do not support the existence of The Psychic Staring Effect.

**B. Two-Way Table Analysis and the Chi-Square Test**

The teacher may also wish to use the class data to help illustrate the analysis of two-way table data. Generally, when data is tallied into a two-way table, we wish to determine if there is a relationship between the two categorical variables whose values have been tabulated in the table.

In the context of Sheldrake’s experiment, the null hypothesis would be that there is no relationship (no association) between whether the Subject is being Looked at and whether the Subject says ‘yes’. The alternative hypothesis would be that there is a relationship (association) between whether the Subject is being Looked at and whether the Subject says ‘yes’.

Once the class data have been collected a two-way table can be constructed:

Table 2. Two-way table for example class data.

|  |  |  |  |
| --- | --- | --- | --- |
| Cell Counts | Answer of Subject | | Row Totals |
| Status of Looker | Looking | Not Looking |
| Looking | 66 | 68 | 134 |
| Not Looking | 76 | 70 | 146 |
| Column Totals | 142 | 138 | 280 |

The hypothesis test that will be used to analyze the data is the chi-square test and the test statistic formula is:

**** where the Expected Count = .

The test statistic is based upon df =  where *r* = number of rows and *c* = number of columns.

The assumptions for the chi-square test are: (1) The two variables tallied in the table are categorical. (2) Randomization was used in the data collection process. (3) The expected counts are at least 5 in all cells for a  contingency table.

Students will need the expected cell counts in order to calculate the test statistic by hand. The expected cell counts are shown in Table 3.

Table 3. Two-way table of expected cell counts.

|  |  |  |  |
| --- | --- | --- | --- |
| Expected Cell Counts | Answer of Subject | | Row Totals |
| Status of Looker | Looking | Not Looking |
| Looking |  |  | 134 |
| Not Looking |  |  | 146 |
| Column Totals | 142 | 138 | 280 |

After the expected counts have been calculated the test statistic is calculated as:



On the TI-84 calculator, students can use the test statistic value to find the corresponding

p-value. They should select 2nd 🡪 VARS 🡪🡪 ENTER. Within the parentheses, they need to enter the lower bound, upper bound, degrees of freedom. The lower bound will always be the test statistic due to the shape of the chi-square distribution. For the upper bound, students can enter any very large number such as 10000000. The degrees of freedom are found using the formula where *r* is the number of rows in the table and *c* is the number of columns. Note that in a two-by-two table, the degrees of freedom always equal 1.

The p-value for the example class data is approximately .64. Based upon this p-value, the null hypothesis cannot be rejected. Therefore, the data do not provide significant evidence to indicate that there is a relationship (association) between whether the Subject is being Looked at and whether the Subject says ‘yes’. Or, in other words, the data do not support the existence of The Psychic Staring Effect.

**C. The Binomial Test**

The problem can also be framed within the context of a binomial experiment. Recall that a binomial experiment has the following properties:

The experiment consists of *n* identical trials.

Each trial results in one of two outcomes. We call one outcome a success *S* and the other a failure *F*.

The probability of success on a single trial is equal to *p* and remains the same from trial to trial. The probability of a failure is equal to .

The trials are independent.

The random variable of interest is *Y*, the number of successes observed during the *n* trials.

For Sheldrake’s experiment, each trial consists of the Looker either looking or not looking at the Subject and then recording the Subject’s response. We could consider a Success to be the Subject correctly saying he/she is being looked at and a Failure the Subject answering incorrectly. Since randomization is used to determine whether the Looker will look or not look, we can consider the trials to be independent. Our random variable, *Y* is then the number of times the Lookers correctly identify being looked at in the class trials. The random variable *Y* is a binomial random variable with probability of success equal to *p* based upon *n* trials.

The probability mass function for the random variable *Y* is:  for

 and . Note that 

Suppose that we believe Sheldrake’s claim that more than 50% of the Subject responses will be correct. Then we seek to support the research hypothesis that *p* the probability of a correct response is higher than .50. And we wish to test  against

How can the class data be used to decide between the null hypothesis and the alternative hypothesis?

Suppose that  trials of the Subject being looked at have been undertaken and the number of correct Subject responses, *Y*, is recorded. Ask students, with random guessing, how many Subject responses would we expect to be correct? With random guessing, we expect (150)(.50) or 75 correct responses.

Ask students, if, say 100 of the Subject responses are correct () what they would conclude about whether or not The Psychic Staring Effect exists? If the Subjects actually give a correct response 50% of the time, it is not *impossible* to observe  correct responses in a sample of size 150, but it is highly *improbable*. It is much more likely that we would observe  if the alternative hypothesis were true. Thus, we should reject the null hypothesis in favor of the alternative hypothesis if we observed a large enough value of *Y*. This means that extreme values are larger values of *Y*.

In order to discuss the idea of rejecting  in terms of a p-value calculation, for the class experiment, suppose that the observed value of *Y*, the number of correct Subject responses out of 150 is 90.

Ask students to think about how to calculate the p-value. By definition, the p-value is the chance of obtaining the observed sample result or a more extreme result, assuming that the null hypothesis is true. If the null hypothesis is true, then *Y* is a binomial random variable with and  So the p-value will equal:

We can obtain the following expression for the p-value: 

Students can calculate this probability value using the TI-84 calculator by selecting

2nd 🡪 VARS 🡪binomcdf(🡪 ENTER. Within the parentheses, the students need to enter the number of trials, value of *p*, and the value of *y*. So, here, we would have binomcdf(150,.50,89) which gives .9912. So, the p-value is

Ask students to think about what would happen to the p-value for some different possible observed class number of Subject successes. For example, if 100 successes are recorded, then an even smaller p-value will result. If only 50 successes are recorded, the p-value would be larger.

Then have students calculate the p-value for their class result. Have them use the p-value to perform a hypothesis test of  versus and make a conclusion as to whether the class data supports the existence of The Psychic Staring Effect.

For the example class data, there were 66 successes in 134 trials. If the null hypothesis is true, then *Y*, the number of successes is a binomial random variable with and  So the p-value will equal: 

binomcdf(134,.50,65) 

Based upon this p-value, the null hypothesis cannot be rejected. Therefore, the data do not provide significant evidence to indicate that the proportion of the time that someone who is being Looked at can identify that they are being Looked at exceeds .50. Or, in other words, the data do not support the existence of The Psychic Staring Effect.

**IV. Interpret the Results**

The results are interpreted in a similar way for all three activity parts. All three data analyses lead to a large p-value, which in turn failed to support the existence of The Psychic Staring Effect.

If the teacher chooses to complete all three parts of the activity, students will be able to see different ways to analyze the same data. They will see that each analysis lead to the same conclusion: that the class data does not support the existence of The Psychic Staring Effect.

If the teacher chooses to complete only some parts of the activity, students will be able to actively participate in data generation, collection, and analysis, in the context of answering a practical question.

**Assessment**

1. Suppose a new treatment for a certain disease is given to a sample of 200 patients. The treatment was successful for 166 of the patients. Assume that these patients are representative of the population of individuals who have this disease.

(a) Calculate the sample proportion successfully treated.

(b) Determine a 95% confidence interval for the proportion of the population for whom the treatment would be successful. Write a sentence that interprets this interval.

2. An ESP experiment is done in which a participant guesses which of 4 cards the researcher has randomly picked, where each card is equally likely. This is repeated for 200 trials. The null hypothesis is that the subject is guessing, while the alternative is that the subject has ESP and can guess at higher than the chance rate.

(i) What is the correct statement of the null hypothesis that the person does not have ESP?

1. *H*0: *p* = 0.5
2. *H*0: *p* = 4/200
3. *H*0: *p* = 1/4
4. *H*0: *p* > ¼

(ii) The subject actually gets 70 correct answers. Which of the following describes the probability represented by the *p*-value for this test?

1. The probability that the subject has ESP.
2. The probability that the subject is just guessing.
3. The probability of 70 or more correct guesses if the subject has ESP.
4. The probability of 70 or more correct guesses if the subject is guessing at the chance rate.

(iii) Which of the following would be a Type 1 error in this situation?

1. Declaring somebody has ESP when they actually don’t have ESP.
2. Declaring somebody does not have ESP when they actually do.
3. Analyzing the data with a confidence interval rather than a significance test.
4. Making a mistake in the calculations of the significance test.

3. The following table contains data collected to test the relationship between gender and the answer to the question, “With whom is it easiest to make friends?” Using an alpha level of .05, test the following hypotheses:

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  | Opposite Sex | Same Sex | No Difference | Total |
| Female | 58 | 16 | 63 | 137 |
| Male | 15 | 13 | 40 | 68 |
| Total | 73 | 29 | 103 | 205 |

(a) Calculate the expected cell counts and find the chi-square test statistic.

(b) Use the calculator to find the corresponding p-value.

(c) Make a conclusion from the test and interpret the results.

4. The probability that a patient recovers from a certain stomach disease is .80. Suppose that 20 people who have contracted this disease are randomly selected. What is the probability that exactly 14 recover from the disease?

**Answers**

1. (a) The sample proportion is****

(b) The formula to use isS*ample estimate ± Multiplier × Standard error*.The sample estimate is****and the standard error is. For 95% confidence the multiplier is 1.96. The 95% confidence interval is , which is .778 to .882. With 95% confidence, we can say that if the whole population with this disease received this treatment, the proportion successfully treated would be between .778 and .882 (or 77.8% to 88.2%).

2. (i) C

(ii) D

(iii) A

3. (a)

|  |  |  |  |
| --- | --- | --- | --- |
| Expected Counts | Opposite Sex | Same Sex | No Difference |
| Female | 48.79 | 19.38 | 68.83 |
| Male | 24.21 | 9.62 | 34.17 |

(b) cdf(8.515, 100000, 2) = .014

(c) Since .014 is less than .05, reject Ho. At the 5% significance level, there is sufficient statistical evidence to indicate that gender and the ease of finding friends based on sex are dependent (related).

4. Let the random variable, *Y*, be the number of the selected people who recover from the disease. Then *Y* has a binomial distribution with  and  Thus  for  So 

**Possible Extensions**

The parts of this activity are all at GAISE Level C. After completing part A. the instructor could use parts B. and C. as extensions.

**References**

1. *Guidelines for Assessment and Instruction in Statistics Education (GAISE) Report*, ASA, Franklin et al., ASA, 2007. <http://www.amstat.org/education/gaise/>.

2. Assessment questions 1, 2, and 3 from: *Mind on Statistics*. Fourth Edition by Utts/Heckard, 2012. Cengage Learning.

3. Assessment question 4 and some ideas for discussion of the binomial distribution taken from *Mathematical Statistics with Applications 7th Edition* by Wackerly, Mendenhall, and Scheaffer. Thomson\*Brooks/Cole 2008.

**I Always Feel Like Somebody’s Watching Me Activity Sheet**

**Background**

The Psychic Staring Effect (Adapted from: <http://en.wikipedia.org/wiki/Staring>)

The Psychic Staring Effect is the idea that people can sense that they are being stared at and it has been studied heavily, by many different researchers, with different results. In 2003, Rupert Sheldrake wrote the controversial book “The Sense of Being Stared At,” which contained a great deal of anecdotal evidence for the phenomenon: “Many people have had the experience of feeling that they are being looked at, and on turning around find that they really are. Conversely, many people have stared at other people's backs, for example in a lecture theater, and watched them become restless and then turn round.”

After students reported the phenomenon to him in the late 19th century, psychologist Edward B. Titchener suggested that the effect was an illusion, and that when a person turned to check whether they were being watched, the initial movement of their head might attract the focus of somebody behind them who was previously only looking in their general direction. By the time the person had turned their head fully, the second person would be looking directly at them, giving the mistaken impression that they had been staring at them all along.

Rupert Sheldrake (Adapted from: <http://www.sheldrake.org/about-rupert-sheldrake>)

Rupert Sheldrake is a biologist and author of more than 80 scientific papers and ten books. He was among the top 100 Global Thought Leaders for 2013, as ranked by the Duttweiler Institute, Zurich, Switzerland's leading think tank. He studied natural sciences at Cambridge University. He then studied philosophy and history of science at Harvard University, before returning to Cambridge, where he took a Ph.D. in biochemistry (1967).

He has performed research in the area of developmental and cell biology. He has also investigated unexplained aspects of animal behavior, including how pigeons find their way home, the telepathic abilities of dogs, cats and other animals, and the apparent abilities of animals to anticipate earthquakes and tsunamis. He subsequently studied similar phenomena in people, including the sense of being stared at, telepathy between mothers and babies, telepathy in connection with telephone calls, and premonitions. Although some of these areas overlap the field of parapsychology, he approaches them as a biologist, and bases his research on natural history and experiments under natural conditions, as opposed to laboratory studies.

**Goal:**

We want to perform one of Sheldrake’s experiments and we want to see if a statistical analysis of **our** data supports Sheldrake’s claims. We will perform Sheldrake’s ‘Method 1’ which is an experiment with Lookers and Subjects within the same room.

**The Experiment:**

The experiment involves working in pairs. One person is **the Looker** and the other **the** S**ubject**. The Subject sits with his or her back to the Looker and keeps his or her eyes closed. Lookers either look or do not look at the Subjects in a series of 10 trials according to a random sequence. This random sequence can be generated by a random number generator on a calculator or by tossing a fair coin. The Looker stands about 3 feet behind the Subject’s back, and either looks or does not look at the Subject in accordance with the random sequence of trials. To signal the beginning of each trial, the teacher will give a signal to the entire class, so that all trials are performed simultaneously. The teacher will say “Trial one: begin.” (Since all Lookers are following different random sequences of instructions, the teacher’s voice can give no relevant clues to the Subjects). Then for the next trial the teacher will say, “Trial two: begin.” And so on. The Subject then says “looking” or “not looking”, and the Looker records the looking status and the Subject’s response on the Data Collection Sheet. The Subject should not spend long thinking about it, but guess quite quickly; 10 seconds are long enough. The Looker records the Subject’s guess and then proceeds to the next trial. The same procedure is repeated for all 10 trials.

After the series of 10 trials has been completed, the Lookers hand in their Data Collection Sheets. The Lookers and Subjects then trade places. Each new Looker starts with a new data sheet.

**Questions:**

**A. Large-Sample Confidence Interval and Hypothesis Test on a Proportion.**

**1.** If a person can in fact determine whether they are being stared at, then what can we say about the numerical value of the proportion of those being Looked at that should guess correctly and say ‘yes’?

**2.** For the class data:

(a) Identify the sample size.  \_\_\_\_\_\_\_\_\_\_

(b) Identify the number of successes (recall, a trial results in a success if the Subject has correctly identified being Looked at). 

(c) Calculate the sample proportion of those being Looked at who correctly answered ‘yes’.

 \_\_\_\_\_\_\_\_\_\_

## **3.** Construct a 95% confidence interval for the proportion of correct guesses for those being Looked at (that is, the proportion of time that those who were being looked at said ‘yes’).

## (a) give the formula:

## (b) plug the appropriate class data into the formula:

(c) give the confidence interval:

(d) interpret the interval – state whether or not the interval supports The Psychic Staring Effect:

**4.** Does the class data provide significant evidence to indicate that the proportion of ‘yes’ guesses is higher than 50% for those being Looked at?

## 

(a) state the appropriate hypotheses:

(b) summarize the data into an appropriate test statistic:

(c) find the p-value:

(d) report a conclusion in the context of this problem:

(e) in the context of this problem, explain what a type 1 error would be:

(f) in the context of this problem, explain what a type 2 error would be:

**B. Chi-Square Analysis.**

**1.** Construct a two-way table to display the class results.

|  |  |  |  |
| --- | --- | --- | --- |
|  | Answer of Subject | | Row Totals |
| Status of Looker | Looking | Not Looking |
| Looking |  |  |  |
| Not Looking |  |  |  |
| Column Totals |  |  |  |

(a) What percentage of those being Looked at said ‘yes’? \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

(b) What percentage of those not being Looked at said ‘yes’? \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

(c) Do the percentages in (a) and (b) support or refute the existence of a relationship between whether the Subject says ‘yes’ and whether the Subject is being Looked at?

**2.** Does the class data provide significant evidence to indicate that there is a relationship between whether the Subject says ‘yes’ and whether the Subject is being Looked at?

(a) specify the appropriate hypotheses:

(b) calculate the expected count for each of the cells in the table:

|  |  |  |  |
| --- | --- | --- | --- |
|  | Answer of Subject | | Row Totals |
| Status of Looker | Looking | Not Looking |
| Looking |  |  |  |
| Not Looking |  |  |  |
| Column Totals |  |  |  |

(c) use the expected counts from (b) to help calculate the value of the test statistic:

(d) calculate the p-value:

(e) report a conclusion in the context of this problem:

(f) What is the advantage of performing a significance test versus simply comparing the percentages of ‘yes’ answers for those Subjects being Looked at and not being Looked at?

C. Binomial Distribution and Binomial Test.

We want to develop a statistical model for our Sheldrake experiment. Once we have developed a model, we can use it to help determine whether or not our class results support the existence of The Psychic Staring Effect.

(a) Consider all of the cases in which *the Subject was being Looked at*. In considering these cases, can we claim that our experiment consisted of *n* identical trials? Explain why or why not and identify the value of *n* for the class.

(b) What were the two possible outcomes on each of these identical trials?

(c) Which of the outcomes would we consider to be a success?

(d) Would the probability of success, *p*, remain the same from trial to trial? Explain why/why not.

(e) Explain why the trials can be viewed as independent.

(f) Let’s consider the random variable of interest *Y*, to be the number of successes observed during the *n* classtrials. What type of probability distribution does this random variable have?

Now, suppose that we believe Sheldrake’s claim that more than 50% of the Subject responses will be correct thus validating the existence of The Psychic Staring Effect. Then we seek to support the research hypothesis that *p*, the probability of a correct response on each trial is higher than .50 and we wish to test  against

How can we use the class data to decide between the null hypothesis and the alternative hypothesis?

(g) Suppose that  trials of the Subject being looked at have been undertaken and the number of correct Subject responses, *Y*, is recorded. With random guessing on each trial, how many Subject responses would we expect to be correct? \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

(h) Suppose that all 150 of the Subject responses are correct (). What would we conclude about whether or not The Psychic Staring Effect exists? Explain your answer.

(i) What types of values of *Y* would lead to the rejection of the null hypothesis? Large values or small values? \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

(j) For the class experiment, suppose that the observed value of *Y*, the number of correct Subject responses out of 150 was 65.

Recall that, by definition, the p-value is the chance of obtaining the observed sample result or a more extreme result, assuming that the null hypothesis is true. Also recall that extreme means contradictory to the null hypothesis.

If our null hypothesis is true, then *Y* is a binomial random variable with \_\_\_\_\_\_\_\_\_\_ and \_\_\_\_\_\_\_\_\_\_.

So the p-value will equal:  with the values given for *n* and *p* above). Circle the correct inequality.

We can obtain the following expression for the p-value: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

And we can calculate \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ using the TI-84 calculator by selecting

2nd 🡪 VARS 🡪binomcdf(🡪 ENTER.

Within the parentheses, you will need to enter the number of trials, value of *p*, and the value of *y*.

So, here, the p-value is: \_\_\_\_\_\_\_\_\_\_

(k) Now that we have calculated the p-value for 65 successes, what can we say about the

p-value for the following numbers of successes:

If there were 90 successes, the p-value would be LARGER/SMALLER than the p-value that was calculated for 65 successes. Circle the correct choice and explain your choice.

If there were 50 successes, the p-value would be LARGER/SMALLER than the p-value that was calculated for 65 successes. Circle the correct choice and explain your choice.

(l) Does the class data provide significant evidence to indicate that the proportion of ‘yes’ guesses is higher than 50% for those being Looked at?

## 

(i) state the appropriate hypotheses:

(ii) the number of successes for the class was *Y =* \_\_\_\_\_\_\_\_\_\_\_\_\_\_

(iii) calculate the p-value for the class value of *Y*:

(iv)

use the p-value to help make a decision about whether or not the null hypothesis should be rejected and report a conclusion in the context of this problem (be sure to state whether or not our class data support the existence of The Psychic Staring Effect):

Data Collection Sheet

Name of Looker\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

Name of Subject\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

|  |  |  |
| --- | --- | --- |
| **Trial** | **Looker**  **Looking (yes) /**  **Not Looking (no)** | **Subject**  **Says Being Looked At (yes)/**  **Says Not Being Looked At (no)** |
| **1** |  |  |
| **2** |  |  |
| **3** |  |  |
| **4** |  |  |
| **5** |  |  |
| **6** |  |  |
| **7** |  |  |
| **8** |  |  |
| **9** |  |  |
| **10** |  |  |

**Summary:**

|  |  |
| --- | --- |
| Looking | Guess by Subject  Yes No |
| Yes |  |
| No |  |